

Programming Techniques for Supercomputers:

Basics – Parallelism, Scalability and parallel efficiency Basic limitations of parallel computing

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- Identify basic limitations of implementations or algorithms for parallel processing
- Assumptions:
	- § Underlying hardware is perfectly scalable (no saturation effects etc.)
	- Basic workload may have pure serial and pure parallel contributions
	- **N**, workers" have to perform either
		- Eixed amount of work as fast as possible \rightarrow Amdahl's law
- - Increasing amount of work (\sim N) in constant time \rightarrow Gustfson's law
- Metrics:
	- § Parallel speed-up
	- § Parallel efficiency

Basics: Motivation

- Absoulte runtime based view: N workers need $Time(N)$
	- Absolute time to execute the serial ($N = 1$) workload on one worker: $Time (1)$
	- **Basic assumption: workload consists of pure serial (s) and perfectly parallelizable (p)** "timefraction"

$$
Time(1) = Times(1) + Timep(1)
$$

Can not be parallelized

- Relative runtime ("fraction") based view:
	- All runtimes are measured realtive to $Time(1) \rightarrow T(N) = \frac{Time(N)}{Time(1)} \rightarrow T(1) = 1$

• **Serial fraction**
$$
s = \frac{Time_s(1)}{Time(1)}
$$
 -- parallel fraction: $p = \frac{Time_p(1)}{Time(1)}$

$$
T(1) = 1 = s + p
$$

Can not be parallelized

First correction towards reality Purely serial parts limit maximum speedup

<u> Timba d</u>

serial serial

Reality Communication / synchronization / load imbalance…

Limitations of Parallel Computing: Metrics to quantify the efficiency of parallel computing

- **E** Assume $T(N)$ is the time to execute "some workload" with N workers
- How much faster do I execute the given workload on N workers?

$$
\rightarrow \text{Parallel Speed-Up:} \left[S_P(N) = \frac{T(1)}{T(N)} \right]
$$

■ How efficient do I use the workers in average?

$$
\rightarrow \text{Parallel Efficiency: } \left[\varepsilon_P(N) = \frac{S_P(N)}{N}\right]
$$

■ Warning: These metrics are relative to the time (performance) of a single worker \rightarrow These metrics are not performance metrics!

Basic limitations of parallel computing

Amdahl's law ("strong scaling") Gustafson's law("weak scaling") Applying Amdahl's law Limitations beyond Amdahl/Gustafson

Limitations of Parallel Computing: Calculating Speedup in a Simple Model ("strong scaling")

Limitations of Parallel Computing: Amdahl's Law ("strong scaling")

- **Benefit of parallelization is strongly limited by serial part** (s)
	- Maximum Speed-Up which can be attained: lim $\lim_{N \to \infty} S_P(N) = \frac{1}{s}$ &

■ **Parallel Efficiency:**
$$
\varepsilon_p = \frac{1}{s(N-1)+1}
$$

- For large number of workers lim $\lim_{N\to\infty}\varepsilon_P(N)=0$
- Reality: No task is perfectly parallelizable
	- Shared resources have to be used serially
	- Task interdependencies must be accounted for
	- Communication overhead (but that can be modeled separately)

Limitations of Parallel Computing: Extended Amdahl's Law with Communication

■ Assume that $c(N)$ is the communication time when using N processors with $c(1) = 0$

 $\rightarrow T(N) = s + \frac{p}{N} + c(N)$

- Communication time may depend on many factors:
	- § Network topology
	- Communication pattern
	- § Message sizes
	- \blacksquare
- Typical scaling of communication times:
	- Global communication, e.g. barrier: $c(N) = k \log N$
	- Every process sending message over bus based network or serialization of communication in application code: $c(N) = k$ N (see next slide)

Limitations of parallel computing:

Amdahl with (simple) communication Model: Extended Amdahl

Limitations of parallel computing: Amdahl's Law

- Large N limits
	- \blacksquare Amdahl's Law predicts (k=0)

(independent of *N*)

■ At k≠0, our simplified model of communication overhead yields a beaviour of

Limitations of parallel computing: Amdahl´s Law

Limitations of parallel computing: Amdahl´s Law at scale

CPUs

Limitations of parallel computing: Impact of communication is not always as bad…

- Communication is not necessarily purely serial
	- § Non-blocking networks can transfer many messages concurrently factor *Nk* in denominator becomes *k*, which can be added to s (technical measure)
	- § Sometimes, communication can be overlapped with useful work ("asynchronous communication"):

■ But never forget

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Limitations of parallel computing: The "weak scaling" scenario

- **EXTE:** Increasing problem size often mainly enlarges "parallel" workload p
	- Then Speed-up increases with problem size

- For some application fields: Solve problems as big as possible
- \rightarrow Increase (parallel) workload with available workers / processors
- \rightarrow This is called "weak scaling"

Limitation of parallel computing: Increasing Parallel Efficiency ("*weak scaling"*)

§ Assume simple and optimistic scenario: Parallel Workload increases linearly with N, i.e. $p \rightarrow N p$

$$
\Rightarrow T(N) = s + \frac{N p}{N} = s + p
$$

- \rightarrow Runtime stays constant if workload is increased linearly with N
- \rightarrow Performance increases linearly with N
- How long does it take to solve the workload of N processors on 1 processor

 $\Rightarrow T_N(1) = s + N p$

$$
S(N) = \frac{T_N(1)}{T(N)} = \frac{s + N p}{s + p} = \frac{s + N p}{T_S(1)} = s + (1 - s)N
$$

Speed-up increases
linearly with N

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Limitations of parallel computing: Applying Amdahl: Serial & Parallel fraction

Always remember model assumptions:

- Workload consists of
	- purely serial (s) and
	- perfectly parallelizable $(p \rightarrow \frac{p}{N})$ parts
- Scalability is limited by
	- serial fraction or
	- communication overhead (extended Amdahl).
- Impact of shared/saturating hardware resources is not modeled
- **E** How to determine model parameters (s, p) ?
	- § First principles: Complete knowledge of application and hardware parameters required too complex for most applications/kernels
	- Fit model parameters to speedup measurements

Limitations of parallel computing: Applying Amdahl: Serial & Parallel fraction

- Naïve approach: Measure performance as a function of cores and fit (extended) Amdahl's law (cf. slide 6/9)
- Hypothetical study on Emmy (i.e. 2-sockets 10 core each per node) extended Amdahl

Limitations of parallel computing: Applying Amdahl: Serial & Parallel fraction

- Better approach: Separation of concerns! Use well-defined basic building blocks as "workers", which
	- are perfectly scalable (no shared resource in between)
	- restrict measured effects to model assumptions, e.g. use full nodes only (one communication path, serial fraction still visible)

Limitations on parallel computing: Applying Amdahl: A more general view

- § Amdahl's law can also be interpreted as follows
	- A fraction p of a given code/workload can be "accelerated" by a factor N through some "acceleration technique"
	- **The remainder part s cannot be accelerated, i.e.** $s + p = 1$
	- **•** "Normalized" runtime of baseline code $T_{base} = 1$ (slide 6: $T(1)$)
	- **•** "Normalized" runtime of accelerated code $T_{acc}(N, s) = s + p/N$ (slide 6: $T(N)$)
- The speed-up of the acceleration technique is

$$
S_p(N) = \frac{T_{base}}{T_{acc}(N,s)} = \frac{1}{s + \frac{1-s}{N}}
$$

- § Potential "Acceleration factors"
	- **Parallel processing with N processes assuming perfect speed-up on fraction** p
	- **Using an accelerator (e.g. GPGPU) which executes the fraction** p **of a code** N **times faster**
	- **Implementing a code transformation which speeds up a fraction** p **of a code by N times**

Limitations on parallel computing: Applying Amdahl: A more general view

Application: GPGPU accelerated code

- Execution time of original code on host: T_{base}
- § "Accelerated execution" (offload)
	- A fraction p of the original code can be executed on GPGPU *N* times faster than CPU
	- \blacksquare The remaining part s is executed on host

 $\Rightarrow S_p(N) = \frac{1}{s+1}$ $\sqrt{\frac{1-s}{N}}$

§ Consider data transfer between host and accelerator: Extended Amdahl's law

$$
\Rightarrow S_p(N,k) = \frac{1}{s + \frac{1-s}{N} + k}
$$

 $\Rightarrow k = \frac{15}{150} = 0.1$ \rightarrow $S_{0.75}$ (15,0.1) = 2,5

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Limitations of parallel computing – beyond Amdahl/G. Shared/saturated hardware resources

■ Saturations of shared hardware resources set limits to scalability not covered by Amdahl's / Gustafson's law

■ Other potential HW bottlenecks: QPI, PCIe, networks (see next lecture)

Limitations of parallel computing – beyond Amdahl/G. Synchronization points and load imbalance

time ■ Load imbalance between "workers" \rightarrow p/N assumption no longer valid (in general) work work wait work wait ■ Hard to model in a general way, but there are important special cases: work wait § A few "laggers" waste lots of resources Sync point § A single (consistent) lagger could be modeled by increased serial fraction work wait work • A few "speeders" may be harmless work work \rightarrow turning some "laggers" into "speeders" may boost performance a lot!Sync point